

# BIG IDEAS FROM QUANTUM MECHANICS:

- Everything is both a wave and a particle. These are dual descriptions of matter and forces.

$$E = hf = \frac{hc}{\lambda} = \frac{h}{2\pi} (2\pi f) = \hbar \omega$$

↑
←
↑

Plank's Constant

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s} = 4.136 \times 10^{-15} \text{ eV}\cdot\text{s}$$

"electron volts"

- Einstein's analysis of the photo-electric effect used this relation for light. He predicted the outcome some 10 yrs. before R.A. Millikan verified it experimentally.
- Max Plank invented "h" as a constant to fix a troubling calculation with what is called a "black body".

• Note:

$$E = pc \quad \left( \begin{array}{l} \downarrow \text{momentum} \\ \leftarrow \text{speed of light} \end{array} \right)$$

$$E = \frac{hc}{\lambda} \quad \rightarrow \quad p = \frac{h}{\lambda}$$

also true for matter waves  
DE BROGLIE RELATION.

- Particles described by wavefunction  $\psi$  which is complex-valued and is a sort of square-root of a probability density

$$\int_{-\infty}^{\infty} \psi^*(x) \psi(x) dx = 1 \quad \left( \text{for one-dim'l motion} \right)$$

$$\frac{-\hbar^2}{2m} \frac{d^2\psi}{dx^2} + U(x)\psi(x) = E\psi(x)$$

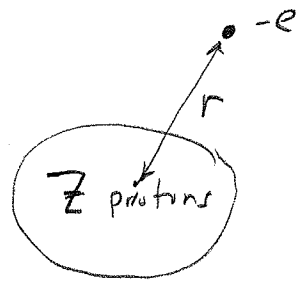
TIME-INDEPENDENT SCHRÖDINGER EQ.

$U(x)$  = potential energy.

Example:

$$U(r) = -\frac{kZe^2}{r}$$

electronic PE for electron in a hydrogen-like atom



$$\Rightarrow E_n = -Z^2 \frac{E_0}{n^2}, n=1,2,3,\dots$$

$\Rightarrow$  Lyman, Balmer, Paschen series as electrons change energy level there is a photon emitted

• FERMIONS: cannot occupy identical set of quantum #'s  $\Rightarrow$  electrons fill up orbitals then no other electrons can also reside in said level.

• BOSONS: can occupy same quantum state as other bosons... like laser light etc...

# Mass / Energy Equivalence

(125)

$$E = \gamma mc^2 \quad \text{where} \quad \gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$

This is the total energy for a particle with rest mass  $m$  and speed  $v$

$$\gamma = (1 - v^2/c^2)^{-1/2} \approx 1 + \frac{1}{2} \left( \frac{v^2}{c^2} \right) + \dots \quad \text{binomial series,}$$

$$\text{Thus, } E = mc^2 \left( 1 + \frac{1}{2} \left( \frac{v^2}{c^2} \right) + \dots \right)$$

$$E = mc^2 + \frac{1}{2}mv^2 + \dots \quad \text{for } v \ll c$$

this approximation is best.

Naturally we identify  $\frac{1}{2}mv^2 = KE$ , but the  $mc^2$  term is new. This is the so-called rest-energy of the particle. This discovery of Einstein is an important part of most of modern physics.

Example: TOTAL NUCLEAR BINDING ENERGY

$$E_B = (ZM_H + Nm_n - M_A)C^2$$

$$E_B + M_A C^2 = ZM_H + Nm_n$$

energy of bound nucleus with mass #  $A$




mass of  $Z$  free hydrogen atoms which is same as  $Zp \oplus Ze^-$   
& mass of  $N$  free neutrons.

( $A = \#$  of total "nucleons" =  $N + Z$ .)  $\nearrow$  (happy?)  
 $\uparrow$   
atomic #

Defn/ Atomic mass unit "u" is defined to be  $\frac{1}{12}$  the mass of a  $^{12}\text{C}$  atom.  
 $(1\text{u})c^2 = 931.5 \text{ MeV}$

Recall  $eV = 1.602 \times 10^{-19} \text{ J}$   
 energy to move one electron over a potential change of 1 Volt.

Examples of rest energy (mass)

$^4\text{He}$		4.002603 u
$^1\text{H}$		1.007825 u
N		1.008665 u

Example

$$2M_{\text{H}} + 2M_{\text{n}} = 4.032980 \text{ u} \neq M_{^4\text{He}}$$

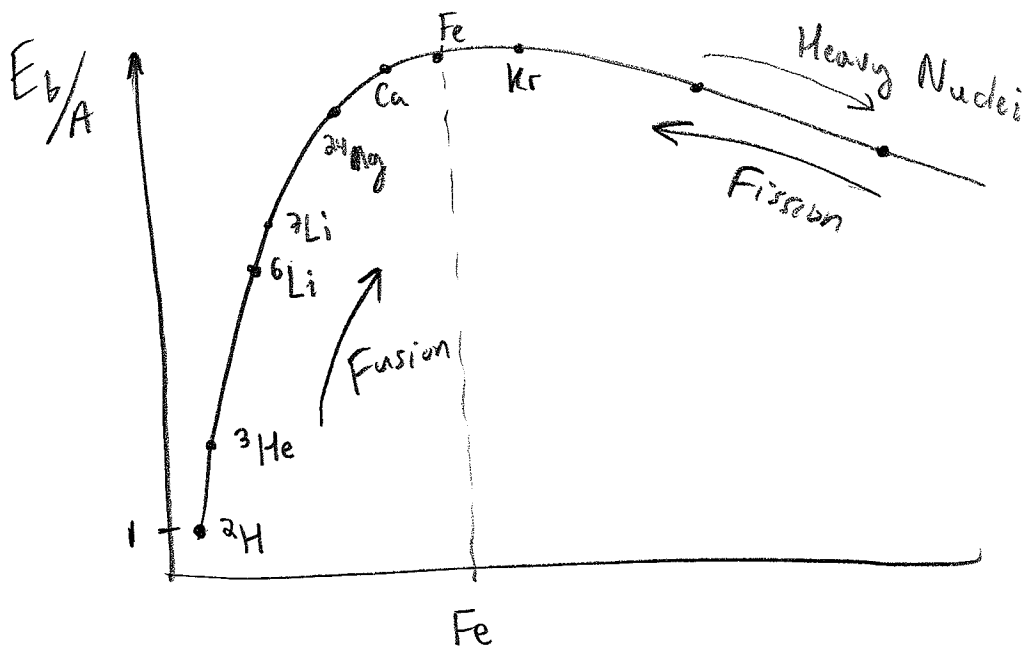
Includes both  $\text{p}$  and  $\text{e}^-$  orbiting  $\text{p}$

$$M_{^4\text{He}} - 2M_{\text{H}} - 2M_{\text{n}} = \underbrace{0.030377 \text{ u}}_{\text{Binding Energy}}$$

$$E_{\text{B}} = (0.030377 \text{ u} c^2) \left( \frac{931.5 \text{ MeV}}{1 \text{ u} \cdot c^2} \right)$$

$$E_{\text{B}} = 28.3 \text{ MeV}$$

(this is an example with  $A=4, Z=2, N=2$  for general formula on (125))



- To minimize energy of Nucleus as a whole you want  $E_b/A$  to be as large as possible since this indicates the depth of the potential well the atom as a whole is occupying in its bound state.

- Fusion combines light nuclei to release mass-energy.
- Fission splits heavy nuclei to release mass-energy.

The shape of curve is result of battle between EM force and the strong force which is very short range. Class cooperating we'll do a thought experiment about this.

Radioactive Decay: unstable states change to lower energy stable states by

$$dN = -\lambda N dt$$

↑  
decay constant

← where N = # of particles.

$$R = -\frac{dN}{dt} = \lambda N$$

$$\tau = \frac{1}{\lambda} = \text{mean lifetime} ; (\ln(2)T = 10.8 \text{ min for free neutron})$$

$$1 \text{ count per second} = 1 \text{ Bq} = 1 \text{ "becquerel"}$$

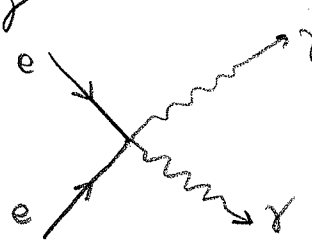
$$1 \text{ Ci} = 3.7 \times 10^{10} \frac{\text{decays}}{\text{second}}$$

a Curie is huge

TYPES OF RADIATION

$\alpha$ :  ${}^{232}\text{Th} \rightarrow {}^{228}\text{Ra} + \alpha = {}^{228}\text{Ra} + {}^4\text{He} \quad (4.08 \text{ MeV})$   
↑ actually He split off the parent atom.  
gives chains  $4n, 4n+1, 4n+2, 4n+3$ .  
(half lives vary  $10^{-5} \rightarrow 10^{10}$  y.)

$\beta$ : too many neutrons / or too few. We (0.782 MeV)  
have A constant but Z changes.  
by either  $\beta^+$  or  $\beta^-$  decay. ( $N \rightleftharpoons P$ )  
 $n \rightarrow p + e^- + \bar{\nu}_e$   
↑ electron neutrino.

$\gamma$ :  $e^+ + e^- \rightarrow \gamma + \gamma$   
electron, positron annihilation  
  
↑ high energy photons.