

NAME _____

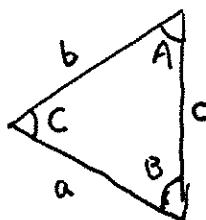
MATH 114: FALL 2021

QUIZ 4 (10PTS+4PTS BONUS)

You may use your homework solutions. I need to look at your class notes while you take this. You are allowed a 3x5 inch card of formulas. Thanks! 2pts per problem.

Problem 1: Simplify $\cos 41x \sin x + \sin 41x \cos x = \boxed{\sin(41x+x)} = \boxed{\sin(42x)}$

Problem 2: If a triangle has interior angles $A = 10^\circ$, $B = 50^\circ$, $C = 120^\circ$ and the length of the side opposite A has length $a = 3$ then find the length of side b opposite B and the length of c opposite C . hint: use the law of sines.

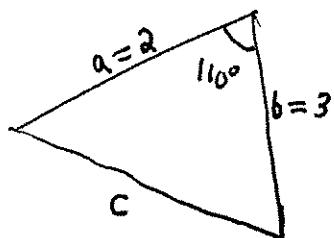


$$\frac{\sin(10^\circ)}{3} = \frac{\sin(50^\circ)}{b} = \frac{\sin(120^\circ)}{c}$$

$$b = \frac{\sin(50^\circ)}{\sin(10^\circ)}(3) \approx \boxed{13.23}$$

$$c = \frac{\sin(120^\circ)}{\sin(10^\circ)}(3) \approx \boxed{14.96}$$

Problem 3: A triangle has side lengths $a = 2$, $b = 3$ and the angle between sides a, b is 110° . Find the length of the remaining side. hint: use the law of cosines.

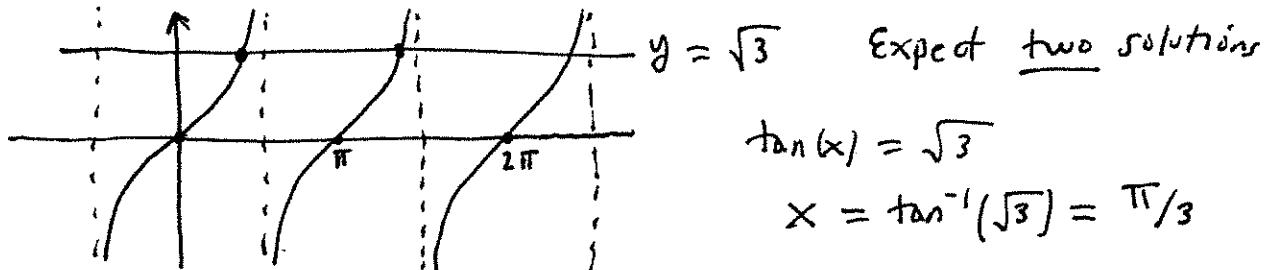


$$c^2 = a^2 + b^2 - 2ab \cos(110^\circ)$$

$$c^2 = 4 + 9 - 2(2)(3) \cos(110^\circ)$$

$$c = \sqrt{13 - 12 \cos 110^\circ} \approx \boxed{4.14}$$

Problem 4: Solve $\tan x = \sqrt{3}$ for $x \in [0, 2\pi]$



To obtain and solution, recall $\tan(x+n\pi) = \tan(x) \quad \forall n \in \mathbb{Z}$. We see from graph, so 1st's are $x = \frac{\pi}{3}, \frac{\pi}{3} + \pi$

$$x = \frac{\pi}{3} \quad \text{and} \quad x = \frac{4\pi}{3}$$

$$\underline{\sec^3(x) - \sec(x) = \sec(x)[\sec^2 x - 1] = \sec x \tan^2 x}.$$

$$\underline{\tan^2 x + 1 = \sec^2 x}$$

Problem 5: Simplify $\sec^3 x + \tan^2 x \sec x$.

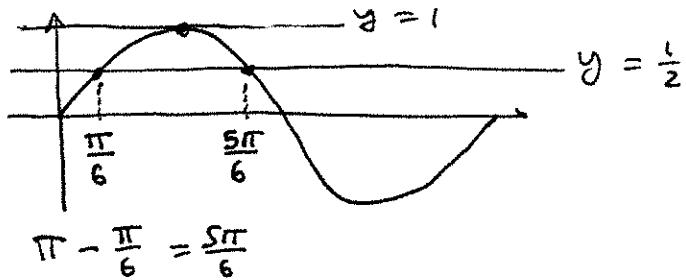
$$\begin{aligned}\sec^3(x) + \sec(x)\tan^2(x) &= \sec(x)[\sec^2(x) + \tan^2(x)] \\ &= \sec(x)[\tan^2 x + 1 + \tan^2 x] \\ &= \underline{\sec(x)[2\tan^2 x + 1]}.\end{aligned}\quad (\text{many correct answers here.})$$

Problem 6: Solve $-2\cos^2 x - 3\sin x + 3 = 0$ for $x \in [0, 2\pi)$ $\cos^2 x + \sin^2 x = 1 \Leftrightarrow \underline{\sin^2 x - 1 = -\cos^2 x}$

$$2(\sin^2 x - 1) - 3\sin x + 3 = 0$$

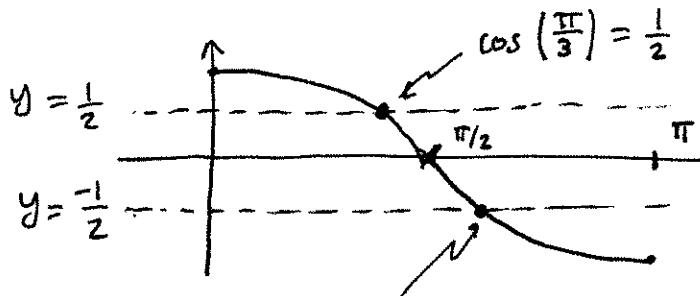
$$2\sin^2 x - 3\sin x + 1 = 0$$

$$(2\sin x - 1)(\sin x - 1) = 0 \quad \begin{array}{l} \sin x = \frac{1}{2} \Rightarrow x = \frac{\pi}{6}, \frac{5\pi}{6} \\ \sin x = 1 \Rightarrow x = \frac{\pi}{2} \end{array}$$



Problem 7: Solve $\sec^2 \theta = 4$ for $\theta \in [0, \pi]$.

$$\frac{1}{\cos^2 \theta} = 4 \Rightarrow \cos^2 \theta = \frac{1}{4} \Rightarrow \underline{\cos \theta = \pm \frac{1}{2}}.$$



$$\pi - \frac{\pi}{3} = \frac{2\pi}{3} \quad \therefore \quad \underline{\theta = \frac{\pi}{3} \text{ or } \frac{2\pi}{3}}$$