

Your solutions should be neat, correct and complete. Same instructions as Mission 1 apply here.

**Recommended Homework from Textbook:** problems:

Chapter 38 #'s 3, 13, 23, 29, 31

**Suggested Reading** the following resources may be helpful:

(a.) Chapter 38 of the required text.

**Problem 73:** (2pts) What famous null result helped make many lose faith in the concept of aether ?

**Problem 74:** (2pts) What are the two basic Axioms of Einstein's Theory of Special Relativity ?

**Problem 75:** (2pts) What is General Relativity and how is it different than Special Relativity ? What technology requires a General Relativistic correction for accuracy ?

**Problem 76:** (2pts) Suppose a space train going  $v = c/2$  with respect to frame  $S$ . This space train has a bike rider who rides on the train at  $v_2 = c/2$  with respect to the frame of reference of the train. What is the observed velocity of the bike with respect to  $S$  ?

**Problem 77:** (2pts) A given elementary particle is seen to last an average of 20 times as long as its usual lifetime as it is shot with high speed  $v$  from a particular high energy accelerator. What is the typical speed  $v$  of these particles ? (give answer in terms of speed of light  $c$ )

**Problem 78:** (2pts) A proton has  $v = c/9$  find the relativistic kinetic energy of the proton and find its relativistic momentum.

**Problem 79:** (2pts) If a particle has relativistic kinetic energy which is 100 times its rest energy then how fast is the particle moving ?

**Problem 80:** (2pts) Suppose event  $E1$  has  $t_1 = 10\text{ s}$  and  $x_1 = 10\text{ m}$  and event  $E2$  has  $t_2 = 20\text{ s}$  and  $x_2 = 10\text{ m}$ . Consider a frame of reference  $S' : (t', x')$  which moves in the usual way at a velocity of  $v = c/99$ . Find the spacetime coordinates of  $E1$  and  $E2$  with respect to the  $S'$ -observer. Of what is this an example ?

**Problem 81:** (2pts) Suppose event  $E1$  has  $t_1 = 10\text{ s}$  and  $x_1 = 10\text{ m}$  and event  $E2$  has  $t_2 = 10\text{ s}$  and  $x_2 = 20\text{ m}$ . Consider a frame of reference  $S' : (t', x')$  which moves in the usual way at a velocity of  $v = c/99$ . Find the spacetime coordinates of  $E1$  and  $E2$  with respect to the  $S'$ -observer.

**Problem 82:** (2pts) Show time dilation with the appropriate spacetime diagram

**Problem 83:** (2pts) Show length contraction with the appropriate spacetime diagram

**Problem 84:** (2pts) In the study of Spacetime in Special Relativity most physical equations are based on using the Minkowski metric. It is defined by:

$$g(\bar{v}, \bar{w}) = -v_0w_0 + v_1w_1 + v_2w_2 + v_3w_3$$

where  $\bar{v} = \langle v_0, v_1, v_2, v_3 \rangle$  and  $\bar{w} = \langle w_0, w_1, w_2, w_3 \rangle$ .

(a.) If  $\bar{v} = \langle ct, ct, 0, 0 \rangle$  then show  $g(\bar{v}, \bar{v}) = 0$ .

(b.) Let  $E_1, E_2$  be events as observed in frame  $S$  and  $E'_1, E'_2$  be the events observed in a frame  $S'$  which moves with velocity  $v$  in the  $x$ -direction in the  $S$ -frame. Show  $g(E_2 - E_1, E_2 - E_1) = g(E'_2 - E'_1, E'_2 - E'_1)$  where  $E_1 = (ct_1, x_1, y_1, z_1)$  etc.